MEM6810 Engineering Systems Modeling and Simulation 工程系统建模与仿真

Theory Analysis

Lecture 6: Verification and Validation of Simulation Models

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- Verification (检验): building the model correctly.
 - Is the desired model implemented correctly in computer (e.g., simulation software, programming language)?
- Validation (验证): building the correct model.
 - Is the simulation model an accurate representation of the real system?



- Repeated steps in model building:
 - Observe the real system.
 - collecting data
 - consult domain experts
 - Construct a conceptual model.
 - assumptions about the system
 - hypotheses about the parameter values
 - Implement an operational model.
 - using simulation software or programming language

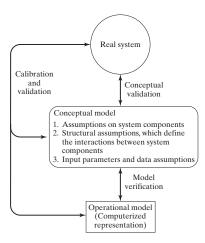


Figure: Model Building Process (from Banks et al. (2010))



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 - To produce a model that represents true behavior closely enough for decision-making purposes.
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- It is the job of the model developer to work closely with the end users throughout the period of development.



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 - If the operational model is animated, verify that what is seen in the animation imitates the actual system.

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 - If the utilization of one station is unreasonably low (or high), it may indicate some possible mistakes in parameters and/or model logic.
 - It may be possible to set the input and/or logic (e.g., Poisson arrival, exponential service time, FCFS) so that the complex queueing network becomes a Jackson queueing network.
 - Compare the analytically solved limiting distribution and $L,\,W,\,L_Q,\,W_Q$ with the simulation results.



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 - Use some sets of data for calibration and other independent sets for "final" validation.



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 - The modeler must weigh the possible, but not guaranteed, increase in model accuracy versus the cost of increased validation effort.
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 - The level of model detail should be consistent with the type of data available.
- Widely used approaches in the validation process:
 - Build a model that has high face validity (表面效度).
 - Validate model assumptions.
 - Compare the model input-output transformations with the actual system's data.



► Build High Face Validity

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- The potential users of a model should be involved:
 - to ensure that a high degree of realism is built into the model;
 - to check a model's face validity e.g., whether the model behaves in the expected way when one or more input variables is changed?
 - Example: In most queueing systems, if the arrival rate of customers increases, it would be expected that server utilization, queue length, and waiting time will increase (although by how much might be unknown).



Validation of Simulation Models ► Validate Model Assumptions

- General classes of model assumptions:
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 - Data assumptions: interarrival times of customers (peak or slack periods), service times (commercial or personal accounts).
 - Verify data reliability with bank managers.
 - Test homogeneity (when combining data) and correlation.
 - Test the goodness of fit for hypothesized distribution.



- Validate the model's ability to predict future behavior.
 - The model is viewed as an input-output transformation.
 - A necessary condition is that some version of the system under study exists.



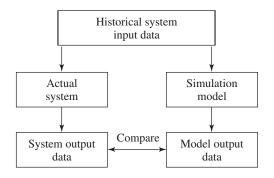
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- Use the main responses of interest as the primary criteria for validating a model.
 - If the model is used later for a different purpose, it should be revalidated in terms of the new responses of interest.



• Input-output validation using historical input data.





- Example: Simulation of a store with 2 parallel servers and 2 waiting lines.
 - It opens at 9 AM and closes at 5 PM every working day.[†]
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 - Simulation model is built based on some assumption and simplification.
 - In actual system, customers may switch waiting lines spontaneously.
 - In simulation model, we assume that customers choose the shortest line when they come and will not change later.
 - Before using the simulation model to answer our question, we first need to validate the model.



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• For each day $i=1,\ldots,K$, we can compute every customer's arrival time and service time (A_{ij},S_{ij}) , and his waiting time $W_{ij},\ j=1,2,\ldots$ We can also get the average waiting time during peak hour, W_i .



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- Suppose the data are reliable, and we can model the arrival (perhaps by a nonhomogeneous Poisson process) and service time with satisfying goodness of fit.
- The remaining issue is on the validity of the structural assumption, i.e., the queue behavior.



- We conduct input-output validation using historical input data.
 - Run the simulation model for K replications, and for each replication $i=1,\ldots,K$, historical data $\{(A_{ij},S_{ij}): j=1,2,\ldots\}$ were fed into the model as input.
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 - Compare system output data $\{W_1, \ldots, W_K\}$ with model output data $\{Y_1, \ldots, Y_K\}$.
 - We are interested in knowing if the two sets of output data are equal statistically.



Input Data Set	System Output W _i	$Model$ $Output$ Y_i	$Observed \ Difference \ d_i$	Squared Deviation from Mean $(d_i - ar{d})^2$
1	W_1	<i>Y</i> ₁	$d_1 = Y_1 - W_1$	$(d_1 - \bar{d})^2$
2	W_2	Y_2	$d_2 = Y_2 - W_2$	$(d_2 - \bar{d})^2$
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	•		•	•
•	•		•	•
			•	
K	W_K	Y_K	$d_K = Y_K - W_K$	$(d_K - \bar{d})^2$
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- Let D := Y W be a random variable of the difference.
 - If the K input data sets are fairly homogeneous, then d_1, \ldots, d_K can be considered as iid realizations of D.
 - It is reasonable to assume that D follows normal distribution.
 - Each Y and W is an average over customers.
 - By the Central Limit Theorem, Y, W, and D are approximately normally distributed when the customer number is large.



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 - The *p*-value is $\mathbb{P}(|T| \ge |t|) = 2 \mathbb{P}(T \ge |t|)$.
 - Under significance level α , reject H_0 if p-value $<\alpha$, or $|t|>t_{K-1,\,1-\alpha/2}$, where $t_{K-1,\,1-\alpha/2}$ is the $(1-\alpha/2)$ -quantile of t distribution with K-1 degrees of freedom.

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- Using historical input in simulation is only recommended for model validation, not for making production run.
- One may also consider to construct a confidence interval for μ to test H_0 .
- When only one data set (instead of K) is available,[†] one needs to use some time-series approaches to compare model output data with system output data.



[†]A common situation in nonterminating simulation (see more details in Lec 7).

► Turing Test

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 - If the manager identifies a substantial number of the fake reports, interview the manager to get information for model improvement.
 - If the manager cannot distinguish between fake and real reports with consistency, conclude that the test gives no evidence of model inadequacy.

